On-the-fly and DAG-aware: Rewriting Boolean Networks with Exact Synthesis

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Abstract—The paper presents a generalization of DAG-aware AIG rewriting for \(k\)-feasible Boolean networks, whose nodes are \(k\)-input lookup tables (\(k\)-LUTs). We introduce a high-effort DAG-aware rewriting algorithm, called cut rewriting, which uses exact synthesis to compute replacements on the fly, with support for Boolean don’t cares. Cut rewriting pre-computes a large number of possible replacement candidates, but instead of eagerly rewriting the Boolean network, stores the replacements in a conflict graph. Heuristic optimization is used to derive a best, maximal subset of replacements that can be simultaneously applied to the Boolean network from the conflict graph. We optimize LUT mapped Boolean networks obtained from the ISCAS and EPFL combinational benchmark suites. For 3-LUT networks, experiments show that we achieve an average size improvement of 5.58\% and up to 40.19\% after state-of-the-art Boolean rewriting techniques were applied until saturation. Similarly, for 4-LUT networks, we obtain an average improvement of 4.04\% and up to 12.60\%.

I. INTRODUCTION

Logic optimization of multi-level Boolean networks plays an important role in automated design flows for digital systems and is responsible for substantial area and delay reductions [1], [2]. These logic optimizations are typically carried out on a simple and technology-independent representation of the digital logic. Particularly, homogeneous data-structures, such as and-inverter graphs (AIGs) [3], [4]—being composed of two-input ANDs and inverters—or majority-inverter graphs (MIGs) [5]—being composed of majority-of-three gates and inverters—have been proven to be successful. Structural hashing on the intermediate representation ensures that no two nodes have identical incoming edges. Arbitrary Boolean networks can be transformed into AIGs or MIGs, for which a repertoire of scalable optimization techniques is available [6].

Boolean rewriting is an optimization technique that iteratively selects small parts of the Boolean network and replaces them with more compact implementations in order to reduce the overall number of nodes, while maintaining the global output functions of the Boolean network. An efficient implementation of this idea is DAG-aware AIG rewriting [7], which exploits structural hashing to find beneficial replacements that utilize the existing logic within the network. Being DAG-aware allows one to obtain a gain even when replacing a smaller part of logic by a larger one, by reusing already existing logic in the network. An efficient implementation of cut enumeration [8], [9], [10] in combination with fast truth table computations and a database of pre-computed replacements for a large number of Boolean functions makes the technique scalable.

In this paper, we generalize DAG-aware rewriting and present a DAG-aware rewriting algorithm that is directly applied to \(k\)-feasible Boolean networks (instead of AIGs). Replacements are computed on the fly using exact synthesis. Exact synthesis offers a more flexible, general, and scalable solution compared to a pre-computed database, and recent achievements in SAT-based exact synthesis enable its integration as an efficient engine in various logic synthesis applications [11]. As a consequence, the proposed approach is generic and capable of optimizing all common technology-independent logic representation including AIGs, MIGs, and XOR-based representations, as well as allows one to obtain size optimizations after technology mapping, e.g., in LUT mapping for FPGAs. Moreover, on the fly synthesis allows us to support don’t care conditions, for which pre-computing a database is intractable. The approach is particularly useful as a post-optimization techniques when other resynthesis techniques saturate.

We call the new algorithm cut rewriting. The algorithm operates in two phases. In the first phase, a large number of possible replacement candidates is computed, but instead of eagerly rewriting the Boolean network, they are stored in a conflict graph. A node of the conflict graph denotes a possible replacement labeled with its achieved node reduction. An edge between two nodes denotes a conflict between two replacements such that only one of them can be applied. In the second phase, the conflict graph is used to determine a globally optimal subset of replacements by solving a maximum weighted vertex independent set problem. Note that, while we use exact synthesis to compute optimum replacement networks, the global optimization flow is heuristic.

We have implemented cut rewriting in a generic C++17 open source Boolean network library and applied it to the ISCAS and EPFL combinational benchmarks. Experiments show that we achieve a reduction of 5.58\% on average and up to 40.19\% when resynthesizing 3-LUT networks. This is after state-of-the-art Boolean rewriting techniques, using the most effective optimization scripts for \(k\)-feasible Boolean networks in ABC [12], were applied until saturation. Similarly, for 4-LUT networks we achieve an average reduction of 4.04\% and up to 12.60\%.

II. PRELIMINARIES

A. Boolean networks

A Boolean network \(N\) is a directed acyclic graph (DAG). Each node corresponds to a logic gate. Each directed edge \((n, m)\) is a wire connecting node \(n\) with node \(m\). The fanin, respectively fanout, of a node \(n \in N\) are the incoming, respectively outgoing, edges of the node. A Boolean network is \(k\)-feasible if the fanin size of all nodes is bounded by \(k\).
A $k$-LUT network is the most general $k$-feasible network in which each gate can implement an arbitrary Boolean function. The primary inputs (PIs) are the nodes of the Boolean network without fanin. The primary outputs (POs) are the nodes of the Boolean network without fanout. All other nodes in the Boolean network are gates.

B. Cuts

A cut of a Boolean network is a pair $(n, L)$, where $n$ is a node, called root, and $L$ is a set of nodes, called leaves, such that 1) each path from any PI to $n$ passes through at least one leaf and 2) for each leaf $l \in L$, there is at least one path from a PI to $n$ passing through $l$ and not through any other leaf. The cover $\text{Cover}(n, L)$ of a cut $(n, L)$ is the set of all nodes $n \in N$ that appear on a path from any $l \in L$ to $n$ including $n$, but excluding the leaves.

A fan-out free cone (FFC) of a node $n$ is a cut $c = (n, L)$ such that no node $n' \in \text{Cover}(n, L)$ with $n' \neq n$ has a parent node that is outside of $\text{Cover}(n, L)$. The maximum fanout-free cone (MFFC, [8]) of a node $n$ is its largest FFC. Informally, the MFFC of a node contains all the logic used exclusively by the node. When a node is removed or substituted, the logic in its MFFC can be removed [10].

C. Exact synthesis

Exact synthesis is the problem of finding the optimum Boolean network given a specification, where network optimality is defined with respect to some cost function. For example, we may want to find the network with the smallest number of nodes when we are optimizing for area, or the network with the fewest logic levels when optimizing for delay.

In recent years, there has been a substantial research effort into solving this problem using SAT based methods [13], [14], [15], [11]. Given an $m$-tuple of functions $f_1(x_1, \ldots, x_n), \ldots, f_m(x_1, \ldots, x_n)$ over $n$ variables, we can encode the following question as a SAT formula $F_r$, [16], [17]:

$$\text{Does there exist a Boolean network $N$ which implements $f_1, \ldots, f_m$ using $r$ gates?}$$

If $F_r$ is SAT, then such a network exists. The satisfying assignment corresponds to a network that implements the functions using $r$ gates. Conversely, if $F_r$ is UNSAT, then we have proven that no such network exists. Hence, if we initialize $r$ to 0 and increment it until we find a satisfiable $F_r$, we can use a SAT solver to find a provably size-optimum Boolean network for $f_1, \ldots, f_m$. This process of size-optimum exact synthesis is illustrated in Fig. 1. More generally, we can re-formulate the above question with arbitrary cost functions $C$.

$$\text{Do there exist a Boolean network $N$ which implements $f_1, \ldots, f_m$ such that $C(N) = r$?}$$

There exist different ways of encoding the exact synthesis problem as SAT formulae, each having their own trade-offs. Some have fewer variables than others, but they may do so at the cost of adding more clauses. Unfortunately, there exists no comprehensive comparison of the differences in runtime.

Algorithm 1: Cut enumeration

Input: Boolean network $N$, cut size $l$, cut limit $p$
Output: Sorted list $C(n) = \{L_1, \ldots, L_p\}$ of leaves for every node $n \in N$
foreach input $n$ in $N$ do Set $C(n) \leftarrow \{\{n\}\}$; foreach gate $n$ in $N$ in topological order do
  let $n_1, n_2, \ldots, n_m$ be the fanin nodes of $n$;
  foreach $L_1 \in C(n_1), L_2 \in C(n_2), \ldots, L_m \in C(n_m)$ do
    Set $L = L_1 \cup L_2 \cup \cdots \cup L_m$;
    if $|L| \geq l$ then continue;
    if $\exists L' \in C(n) : L' \subseteq L$ then continue;
    Remove all $L'$ from $C(n)$ for which $L \supset L'$;
    Insert $L$ into $C(n)$ and keep $C(n)$ sorted;
    if $|C(n)| > p$ then
      Remove the last $|C(n)| - p$ elements from $C(n)$;

A. Cut enumeration

The proposed rewriting algorithm makes use of cut enumeration, which is an algorithm that can compute all cuts of all nodes in a Boolean network. Since the number of cuts is very large, the number of enumerated cuts is bounded by a parameter $l$ for the cut size and a parameter $p$ for the maximum number of cuts for each node. This technique is referred to as priority cuts [10] as it selects the subset of all cuts with respect to some cost function, in our case the number of the cuts' leaves. The returned cut sets are also irredundant and do not contain two cuts $(n, L_1)$ and $(n, L_2)$ such that $L_1$ dominates $L_2$, i.e., $L_1 \subseteq L_2$.

Algorithm 1 sketches the cut enumeration procedure that is used in the rewriting algorithm. It omits details on truth table computation and cut pruning based on functional dependence. The algorithm returns on termination a map from node $n$ to
a sorted list of leaves \( C(n) \) such that every pair \((n, L)\) for \( L \in C(n) \) is a cut of the Boolean network. In addition to basic cut function computation, we also compute the cut function’s Boolean controllability don’t cares, which are based on the local structure of the logic network.

### B. DAG-aware rewriting

In this section, we review an efficient algorithm to compute the gain of replacing a part of logic in a network by another part of logic [7].

The algorithm to compute the gain makes use of reference counting and assigns a value to each node in the network. These values are initialized with the nodes’ fanout sizes. New nodes that are added to the network for a possible replacement will be assigned a reference count of 0. The reference count of a node indicates how many other nodes require this node in the network. In particular, a reference count of 0 means that the node is not required in the network. The algorithm also exploits structural hashing, i.e., nodes from a replacement candidate that are already in the network will not be added another time, and also its reference counter will not be changed.

For “simulating” the removal of a node \( n \) from a network, we recursively decrement all predecessors in the transitive fanin of the node and continue as long as the reference counters of a child become 0 or a leaf node is reached. Algorithm 2 shows the details. It receives as inputs the node \( n \) and the leaves of a cut \( L \).

Adding a node to a network can be “simulated” by the inverse algorithm to \( \text{DerefNode} \), called \( \text{RefNode} \) (see Algorithm 3), which will increment reference counters and continue on the predecessors as long as the reference counter was 0 before incrementing it, and stops otherwise or when it reaches a leaf node. Calling \( \text{DerefNode} \) on the top most AND gate changes the references counters as shown in Fig. 2(e). In particular, the OR gate in the middle of the network now has a reference value of 0, meaning it is not required anymore after deleting the cut. Together with the root node this leads to a value of 0 which is returned by \( \text{DerefNode} \). Afterwards the logic for the replacement cut is added in Fig. 2(d). Note that two of the three gates are already present in the network and only one new node is added, which is initialized with a reference value of 0. All other reference values remain the same. Calling \( \text{RefNode} \) on the root node of the inserted cut simulates an insertion of the cut and leads to the reference values as in Fig. 2(e).

The function returns 1 for the increment of the root node. From these two values we can derive that replacing the first cut by the other will save \( 2 - 1 = 1 \) nodes. Since the cost of the replacement should only be calculated and not actually be performed one can undo the changes to the reference counters by simply calling the inverse functions in inverse order, i.e., calling \( \text{DerefNode} \) on the root node of the replacement cut and \( \text{RefNode} \) on the root node of the original cut leading

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**Algorithm 2:** Dereferencing a node

\[
\text{function DerefNode}(n, L) \\
\text{if } n \in L \text{ then return } 0; \\
\text{Set value } \leftarrow 1; \\
\text{foreach child } c \text{ of } n \text{ do} \\
\quad \text{Set ref}(c) \leftarrow \text{ref}(c) - 1; \\
\quad \text{if ref}(c) = 0 \text{ then} \\
\quad \quad \text{Set value } \leftarrow \text{value } + \text{DerefNode}(c, L); \\
\text{return value;}
\]

**Algorithm 3:** Referencing a node

\[
\text{function RefNode}(n, L) \\
\text{if } n \in L \text{ then return } 0; \\
\text{Set value } \leftarrow 1; \\
\text{foreach child } c \text{ of } n \text{ do} \\
\quad \text{Set ref}(c) \leftarrow \text{ref}(c) + 1; \\
\quad \text{if ref}(c) = 1 \text{ then} \\
\quad \quad \text{Set value } \leftarrow \text{value } + \text{DerefNode}(c, L); \\
\text{return value;}
\]

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Fig. 2. Example for estimating the insertion of a replacement cut using reference counters.
function DryReplace(N, n ⨾ n’, L)  
    Set v₁ ← DerefNode(n, L);  
    Insert cut (n’, L) into the network;  
    Set v₂ ← RefNode(n’, L);  
    DerefNode(n’, L);  
    RefNode(n, L);  
return v₁ − v₂;

Algorithm 4: Adding a new cut (n’, L) into the network and calculating the gain when replacing an existing cut (n, L)

function MFFCSize(N, n)  
    Set L ← primary inputs of N;  
    Set v ← DerefNode(n, L);  
    RefNode(n, L);  
return v;

Algorithm 5: Compute the size of the MFFC of n

to the reference values as shown in Fig. 2(f) and Fig. 2(g), respectively.

This example motivates a function called DryReplace(N, n ⨾ n’, L), as shown in Algorithm 4, that inside a network N simulates the replacement of an existing cut (n, L) with a new cut (n’, L) by using reference counters. The algorithm does not change the reference values of existing nodes in N and all newly added nodes will be assigned a reference value of 0. The function returns the gain of replacing the existing cut with the new one. This gain may be negative.

The routines RefNode and DerefNode can also be used conveniently to compute the size of the MFFC of a node, as shown in Algorithm 5. In here, the cut leaves L are the primary inputs in order to find all logic in the node’s MFFC.

C. Cut rewriting

This section describes a rewriting algorithm that finds replacement candidates for all enumerated cuts in a k-feasible Boolean network. Since cuts found by cut enumeration may not be an FFC, DAG-aware rewriting techniques are used to compute the gain of possible replacement candidates. After all replacement candidates and their gain have been computed, the algorithm finds a set of replacement candidates that maximize the overall gain. Algorithm 6 shows a pseudo code for the algorithm, which is explained in detail in the remainder of this section.

The algorithm starts by computing all cuts for a cut size l and cut limit p. The cut size should be chosen according to k. For example, l must be larger than k to find replacement candidates that lead to a gain, but if l is too large it can significantly degrade the success rate of exact synthesis. We experimentally evaluated that for k = 2 and k = 3, cut sizes l = 5 and l = 6 lead to good results, respectively.

Next, an empty graph G is initialized that will be constructed when enumerating replacement candidates for the cuts. The graph has vertices V for cuts, and an edge in E if two cuts have overlapping logic and can therefore not be replaced simultaneously. Also it has a vertex weight w that is assigned the possible gain of a cut when being replaced by its best found replacement. Finally, the mapping r maps a vertex to the root node of the best replacement cut.

For each cut (n, L) the algorithm enumerates possible replacements (n’, L) using SAT-based exact synthesis. The replacements must not necessarily be optimum in size. The runtime of exact synthesis can be controlled by setting thresholds on the conflict limit of the SAT solver [11]. For each replacement candidate the gain is computed using DryReplace and the best gain is stored in a variable gain together with the best replacement candidate in bestReplacement. If a replacement that leads to a gain can be found a vertex for the cut is added to G and the mappings w and r are updated with the gain and the replacement candidate, respectively. Afterwards, edges are added to G for each two cuts that have overlapping covers. To obtain a good subset of non-conflicting replacement candidates we heuristically solve the maximum weighted independent vertex set problem on G with respect to weights w using the greedy algorithm GWMIN [18], which provides an approximation guarantee of finding a solution with a weight of at least $\frac{1}{\Delta} \alpha(G)$, where $\Delta$ is the degree of G and $\alpha(G)$ is the weight of the exact solution.

In order to speed up computation, we apply two effective techniques. First, we skip all nodes whose MFFC size is 1, i.e., the replacement of the node cannot lead to any positive gain. Second, we cache all replacement candidates computed by exact synthesis. That is, for every unique cut function, replacements are only computed once and then stored in a hash table. This table is particularly useful, when calling cut rewriting repeatedly, because successive runs need to call exact synthesis only on new cuts found by cut enumeration.
IV. EXPERIMENTS

We implemented our approach in C++-17 using the EPFL logic synthesis libraries [19] mockturtle\textsuperscript{2} and percy\textsuperscript{3} in a generic way such that it can in principle be applied to any $k$-LUT network. Exact synthesis has the most impact to performance, and our experiments indicate that using the current implementation, practical and scalable results can be achieved.

We applied cut rewriting to improve the size of 3-LUT and 4-LUT networks for the combinational instances in the ISCAS benchmarks and the arithmetic instances in the EPFL benchmarks [20]. The baseline networks are obtained by performing a LUT mapping using \texttt{&if}, \texttt{-if} \texttt{-K} \texttt{k} with \texttt{k} \in \{3, 4\} in ABC [12], respectively. In case of the EPFL benchmarks, we chose the best-known size-optimized 6-LUT benchmarks as a starting point.\textsuperscript{4} As state-of-the-art area optimization we apply a synthesis script that interleaves priority-cut-based LUT mapping (\texttt{&if}) [10], structural choices (\texttt{&dch} and \texttt{&synch2}) [21], [22], and Boolean network optimization and resynthesis (\texttt{&mfs}) [23]. We apply the synthesis script

\begin{verbatim}
&st; &synch2; &if -m -a -K k; &mfs -W 10;
&st; &dch; &if -m -a -K k; &mfs -W 10
\end{verbatim}

with the respective \texttt{k} parameter ten times and pick the best result that was encountered during all iterations. This optimization method is called \texttt{MFS} in the remainder.

We call the proposed cut rewriting algorithm repeatedly until no further gain in area can be achieved. We apply our approach as a post-optimization approach on the optimized networks obtained by MFS.

Tables I and II show the experimental results for 3-LUTs and 4-LUTs, respectively. The table lists the baseline, the results obtained after MFS, and the results obtained by applying cut rewriting after MFS. For each it lists the number of gates and the number of logic levels. It also lists runtime in seconds. In case of \texttt{MFS + Cut rewriting} it only lists the time required by cut rewriting. The last column shows the improvement that can be obtained by calling cut rewriting on the results already optimized by MFS. The cut size and cut limit for cut enumeration are $l = 6$ and $p = 12$, respectively. We compute one replacement candidate for each cut using exact synthesis with a conflict limit of 1000.

The strength of cut resynthesis becomes evident when used as a post-optimization method after MFS has been tried heavily to find the best network. On top of the significantly improved results, cut rewriting can find additional improvement—often even with a comparably small runtime overhead. The average improvement is 5.58\% and 4.04\% when resynthesizing 3-LUT and 4-LUT networks, respectively. The best improvement is achieved for the 128-bit adder, which improved by 40.19\% when considering 3-LUT networks. Starting from a baseline implementation that has 67 logic levels it manages to regain the size-optimal carry ripple implementation with one sum gate (XOR-3) and one carry gate (majority-3) for each pair of input bits.

V. CONCLUSION

We have presented a DAG-aware rewriting algorithm directly applied to $k$-feasible Boolean networks. Instead of using simple transformations, a SAT-based exact synthesis engine with support for Boolean don’t cares is employed for rewriting existing logic. Moreover, instead of applying replacements ad-hoc, all possible gains are stored in a conflict graph, from which a maximal subset of compatible replacements is computed. We show size improvements up to 40.19\% and 12.60\% when resynthesizing 3-LUT networks and 4-LUT networks, respectively. Today’s exact synthesis methods are not strong enough to efficiently find compact 6-LUT networks for functions with 8–10 variables. Improvements to the scalability of exact synthesis can be directly exploited by our proposed approach.

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REFERENCES


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\textsuperscript{3} see github.com/whaaswijk/percy  
\textsuperscript{4} see github.com/lsils/benchmarks
### TABLE I
**EXPERIMENTAL RESULTS FOR 3-LUT RESYNTHESIS**

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### TABLE II
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